

CHEM 101A - Chapter 5 Gas Problems

$$T_K = T_C + 273$$

1. Oxygen gas occupies 573 mL at $50.^\circ\text{C}$. If the temperature is reduced to -78°C , what is the volume of gas, assuming pressure and moles are held constant?

$$\frac{573 \text{ mL}}{323 \text{ K}} = \frac{V_2}{195 \text{ K}}$$

$$V_2 = 345.9287$$

$$\boxed{346 \text{ mL}}$$

2. A sample of an ideal gas is placed in a 20.0-L vessel at STP. The volume is reduced to $500. \text{ mL}$ whilst the temperature is increased to $150.^\circ\text{C}$. Find the pressure.

$$P_1 = 1 \text{ atm} \quad P_2 = ?$$

$$V_1 = 20.0 \text{ L} \quad V_2 = 0.500 \text{ L}$$

$$T_1 = 273 \text{ K} \quad T_2 = 423 \text{ K}$$

$$\frac{T_2}{V_2} \cdot \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \cdot \frac{T_1}{V_1}$$

$$P_2 = \frac{T_2 P_1 V_1}{V_2 T_1} = \frac{(423 \text{ K})(1 \text{ atm})(20.0 \text{ L})}{(0.500 \text{ L})(273 \text{ K})}$$

$$P_2 = 61.9780$$

$$\boxed{P_2 = 62.0 \text{ atm}}$$

3. An unknown elemental gas has a pressure of 722 mm Hg at 100.°C and has a density of 2.60 g/L. What is the identity of the gas? *Hint: if it is a diatomic element, its molar mass is twice its atomic mass!*

$$722 \text{ mmHg} \times \frac{1 \text{ atm}}{760 \text{ mmHg}} = 0.950 \text{ atm}$$

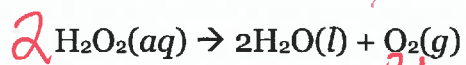
$$MP = dRT$$

$$M = \frac{dRT}{P} = \frac{(2.60 \frac{\text{g}}{\text{L}}) \left(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}\right) (373\text{K})}{0.950 \text{ atm}}$$

$$M = 83.8 \text{ g/mol} = \text{Kr}$$

4. Determine the densities of the noble gases at STP.

5. Concentrated H_2O_2 solutions are explosively decomposed by transition metal catalysts.



What volume of dry O_2 collected @ 27°C and 746 torr could be generated by decomposition of 125g H_2O_2 (50.0% by mass)?

(Sample mass) (% mass) = mass pure

$$(125 \text{g } \text{H}_2\text{O}_2) (0.500) = 62.5 \text{g } \text{H}_2\text{O}_2$$

$$62.5 \text{g } \text{H}_2\text{O}_2 \times \frac{1 \text{ mol } \text{H}_2\text{O}_2}{34.016 \text{ g } \text{H}_2\text{O}_2} \times \frac{1 \text{ mol } \text{O}_2}{2 \text{ mol } \text{H}_2\text{O}_2} = 0.919 \text{ mol } \text{O}_2$$

$$\frac{PV}{P} = \frac{nRT}{P}$$

$$V = \frac{nRT}{P}$$

$$R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}$$

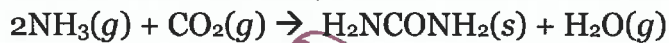
$$P = 746 \text{ torr} \times \frac{1 \text{ atm}}{760 \text{ torr}} = 0.9816 \text{ atm}$$

$$T = 273 + 27 = 300 \text{ K}$$

$$= \frac{(0.919 \text{ mol } \text{O}_2) (0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}) (300 \text{ K})}{0.9816 \text{ atm}}$$

$$= \boxed{23.0 \text{ L } \text{O}_2}$$

6. Urea (H_2NCONH_2) can be synthesized from ammonia and carbon dioxide:



At 223°C , ammonia gas at $90.\text{atm}$ flows into a reactor at a rate of $500.\text{L}/\text{min}$ whilst carbon dioxide gas at 45 atm flows into a reactor at a rate of $600.\text{L}/\text{min}$.

What mass urea is produced per minute at 100% yield?

$$n_{\text{NH}_3} = \frac{PV}{RT} = \frac{(90.\text{atm})(500.\text{L})}{(0.08206\text{ L}\cdot\text{atm}/\text{K}\cdot\text{mol})(496\text{ K})} = 1105.6\text{ mol NH}_3$$

$$n_{\text{CO}_2} = \frac{(45)(600)}{(0.08206)(496)} = 663.4\text{ mol CO}_2$$

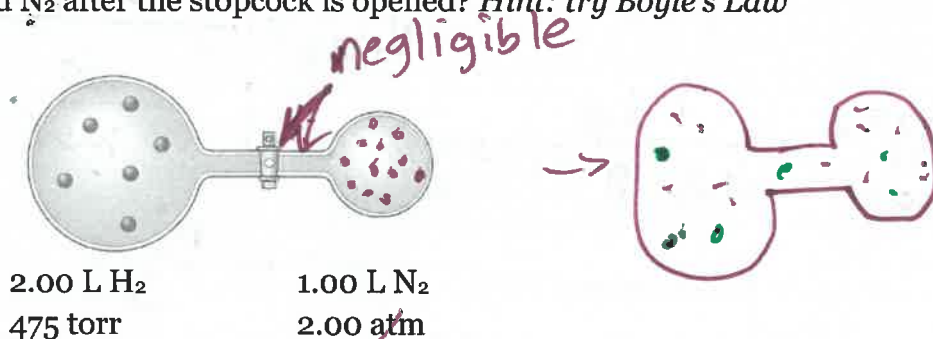
$$1105.6\text{ mol NH}_3 \times \frac{1\text{ mol Urea}}{2\text{ mol NH}_3} \times \frac{60.06\text{ g Urea}}{1\text{ mol Urea}} =$$

$$= 33,202\text{ g Urea}$$

$$= 33,000\text{ g Urea}$$

$$= \boxed{33\text{ kg Urea}/\text{min}}$$

7. Consider the 2-bulbed flask below. What are the final partial pressures (in torr) of H_2 and N_2 after the stopcock is opened? *Hint: try Boyle's Law*



1520 torr

	P_1	V_1	\rightarrow	V_2	P_2	Equation
H_2	475 torr	2.00 L	\rightarrow	3.00 L	? torr	$P_1 V_1 = P_2 V_2$
					\downarrow	$P_{H_2} = 317 \text{ torr}$
N_2	1520 torr	1.00 L	\rightarrow	3.00 L	? torr	$P_{N_2} = 507 \text{ torr}$

$$P_{\text{tot}} = 317 \text{ torr} + 507 \text{ torr}$$

$$= 824 \text{ torr}$$

8. You have two balloons—one filled with hydrogen and one with xenon gas, both at 298K.

a. What is the root mean square velocity of the hydrogen molecules?

$$u_{rms} = \sqrt{\frac{3RT}{M}}$$

UNITS

$$u_{rms} = \frac{\frac{\cancel{\text{kg}} \cdot \frac{\cancel{\text{m}}^3}{\cancel{\text{s}}^3} \cdot \frac{\cancel{\text{K}}}{\cancel{\text{K}}}}{\frac{\cancel{\text{kg}}}{\cancel{\text{mol}}}} = \frac{\text{m}}{\text{s}}$$

$$\frac{2.016 \text{ g H}_2}{\text{mol}} \times \frac{1 \text{ kg}}{1000 \text{ g}} = .002016 \text{ kg/mol}$$

$$u_{rms} = \sqrt{\frac{3 \cdot 8.314 \cdot 298}{.002016}} = \sqrt{3,168,963} = 1920 \text{ m/s}$$

$\sim 4000 \frac{\text{mi}}{\text{h}}$

b. What is the root mean square velocity of the xenon atoms?

$$u_{rms} = \sqrt{\frac{3 \cdot 8.314 \cdot 298}{0.1313}} = 238 \text{ m/s}$$

Same
(KE) avg

SF₆ H₂O
He9. Calculate the average kinetic energy of one molecule of CO₂ at 150°C.

$$\begin{aligned} (KE)_{\text{avg}} &= \frac{3}{2} RT \\ &= \frac{3}{2} \left(8.314 \frac{\text{J}}{\text{K}\cdot\text{mol}} \right) (423 \text{ K}) \\ &= 5280 \frac{\text{J}}{\text{mol}} \times \frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ molecule}} \\ &= \boxed{8.76 \times 10^{-21} \text{ J/molecule}} \end{aligned}$$

10. Calculate the pressure exerted by 1.500 moles of xenon in a 2.000-L flask at a) 200.0K and b) 1000. K, using the ideal gas equation and the Van der Waals equation.

IDEAL
 $T = 200.0\text{K}$ $P = \frac{(1.500)(.082057)(200.0)}{2.000} =$

$T = 1000.0\text{K}$ $P = \frac{(1.500)(.082057)(1000.)}{2.000} =$

VDW

$T = 200.0\text{K}$

$$P = \frac{(1.500)(.082057)(200.0)}{(2.000 - (1.500)(.0511))} - \left(\frac{1.500}{2.000}\right)^2 \cdot 4.19$$

$= 10.44 \text{ atm}$

$T = 1000.0\text{K}$

$$P = \frac{(1.500)(.082057)(1000.)}{(2.000 - 1.500 \cdot .0511)} - \left(\frac{1.500}{2.000}\right)^2 \cdot 4.19$$

$= 61.64 \text{ atm}$